

Name and surname:

U number:

## Calculus I - MAC 2311 - Section 007

### Quiz 5 — Take-home quiz

*Expires on Thursday October 26 at 11 am*

1) [3 points] Without using a calculator compute the following values.

a)  $\sin^{-1}\left(-\frac{\sqrt{2}}{2}\right) =$

b)  $\cos^{-1}\left(\frac{1}{2}\right) =$

c)  $\tan^{-1}(\sqrt{3}) =$

d)  $\sin\left(\cos^{-1}\left(\frac{\sqrt{3}}{2}\right)\right) =$

e)  $\tan^{-1}\left(\sin\left(-\frac{\pi}{2}\right)\right) =$

f)  $\cos^{-1}\left(\sqrt{3}\sin\left(\frac{\pi}{6}\right)\right) =$

2) [1+2.5+1.5 points] Consider the function

$$f(x) = \tan(\sin^{-1}(2x)).$$

a) Find the domain of  $f$ .

b) Show that for each  $x$  in the domain a simplified expression for  $f$  is  $\frac{2x}{\sqrt{1-4x^2}}$ .

c) Compute  $f'(x)$ .

3) [1.5+1.5 points] Compute the following limits and show all your work:

a)  $\lim_{x \rightarrow 0} \frac{x^2}{1 - \cos(x)}$

b)  $\lim_{x \rightarrow \infty} x e^{-x}$